

# SPECIFICATION AND ANALYSIS OF REAL-TIME SYSTEMS IN **REAL-TIME MAUDE**

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## FORMAL METHODS: KEY TRADE-OFF

expressiveness/modeling convenience  $\longleftrightarrow$  analytic power

# REWRITING LOGIC AND MAUDE

- modeling convenience!
- **simple** and **intuitive**
- any data type
- unbounded data structures
- simple model of **concurrent objects**
  - dynamic object/message creation/deletion
  - easy to define forms of communication
- hierarchical structures
  - properties in general **undecidable**
- analysis by system **execution**

(How) can we model and analyze **real-time systems** in rewriting logic so that the advantages of Maude are maintained?

**MODELING AND ANALYZING  
REAL-TIME SYSTEMS WITH  
REAL-TIME MAUDE**

---

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- **fault-tolerant** systems must discover message loss/node crash
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  - toasters
  - cars, airplanes, ...
  - e-banking

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- time key in most systems
  - toasters
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- scheduling algorithms
- **timed models** enable reasoning about **performance**
- **timed properties** important
  - airbag must deploy within **10ms** of a crash

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Why **dense** time ( $\mathbb{R}_{\geq 0}$ ,  $\mathbb{Q}_{\geq 0}$ , ...)?

- “real” real-time system
- techniques useful for discrete-time systems
  - example: events take place approximately once per 10,000 ms

## Real-Time Maude:

- Extends **Maude** to **model** and **analyze** real-time systems
- **Object-oriented** modeling of distributed real-time systems
- Implemented in Maude as an extension of Full Maude
- <http://www.ifi.uio.no/RealTimeMaude>



- **Data types** modeled by algebraic equational specification
  - parametric time domain
  - built-in time domains `NAT-TIME-DOMAIN-WITH-INF`,  
`POSRAT-TIME-DOMAIN-WITH-INF`, ...

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- **Instantaneous** transitions modeled by **rewrite rules**

`cr1 [!] : t => t' if cond`

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- **Instantaneous** transitions modeled by **rewrite rules**

`crl [l] : t => t' if cond`

- **Time advance** modeled **explicitly** by **tick rewrite rules**

`crl [l] : {t} => {t'} in time  $\tau$  if cond`

- global state has form `{t}`
- ensures **uniform** time elapse

# REAL-TIME MAUDE ANALYSIS

- Timed **rewriting**
  - simulate system to time  $T$
- Timed **reachability analysis**
  - find states reachable in time interval
- **LTL** model checking
  - unbounded
  - time-bounded
    - finite reachable state space

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- **Timed CTL** model checking
- “Find earliest” and “find latest” ...

“Time sampling” discretization of dense time (see below)

# MODELING IN REAL-TIME MAUDE

---

# EXAMPLE: "RETROGRADE" CLOCK

- State: `{clock(r)}` or `{stopped-clock(r)}`
- **Dense** time domain
- Clock can stop at **any** time
- **Retrograde** clock: `clock(12)` must be reset to `clock(0)`





# REAL-TIME MAUDE SPECIFICATION

```
(tmod DENSE-CLOCK is pr POSRAT-TIME-DOMAIN .
  ops clock stopped-clock : Time -> System .
  vars R R' : Time .

  crl [tickWhenRunning] :
    {clock(R)} => {clock(R + R')} in time R'
    if R' <= 12 - R [nonexec] .

  rl [tickWhenStopped] :
    {stopped-clock(R)} => {stopped-clock(R)} in time R'
    [nonexec] .

  rl [reset] :   clock(12) => clock(0) .

  rl [batteryDies] :   clock(R) => stopped-clock(R) .
endtm)
```

## NEXT EXAMPLE: SINGLE IMPRECISE CLOCK

- One clock
- Imprecise: goes faster or slower than “real time”
  - given by its rate

# MODELING SINGLE IMPRECISE CLOCK

```
(tomod SINGLE-SKEWED-CLOCK is pr POSRAT-TIME-DOMAIN .

class Clock | running : Bool, time : Time, rate : PosRat .

var C : Oid . vars R R' : Time . var RATE : PosRat .

crl [tickRunning] :
  {< C : Clock | running : true, time : R, rate : RATE >}
=>
  {< C : Clock | time : R + (RATE * R') >} in time R'
  if R' <= (12 - R) / RATE [nonexec] .

rl [tickStopped] :
  {< C : Clock | running : false >} => {< C : Clock | >}
  in time R' [nonexec] .
```

## MODELING SINGLE IMPRECISE CLOCK (CONT.)

```
rl [reset] :  
  < C : Clock | running : true, time : 12 >  
=>  
  < C : Clock | time : 0 > .
```

```
rl [break] :  
  < C : Clock | running : true >  
=>  
  < C : Clock | running : false > .
```

```
endtom)
```

## ANOTHER EXAMPLE: MULTIPLE IMPRECISE CLOCKS

We now model **many** imprecise clocks.

- Instantaneous rules as before
- **Single** tick rule:

```
var CLOCKS : Configuration .   var R' : Time .
```

```
cr1 [tick] :  
  {CLOCKS} => {advanceTime(CLOCKS)} in time R'  
  if R' <= maxTimeAdvance(CLOCKS) .
```

## MULTIPLE IMPRECISE CLOCKS (CONT.)

```
vars CLOCKS CLOCKS' : Configuration .
```

```
op advanceTime : Configuration Time -> Configuration [frozen (1)]
```

```
ceq advanceTime(CLOCKS CLOCKS', R)
  = advanceTime(CLOCKS, R) advanceTime(CLOCKS', R)
  if CLOCKS /= none and CLOCKS' /= none .
```

```
eq advanceTime(< C : Clock | running : true, time : R,
               rate : RATE >, R')
  = < C : Clock | time : R + (R' * RATE) >
```

```
eq advanceTime(< C : Clock | running : false >, R')
  = < C : Clock | > .
```

## MULTIPLE IMPRECISE CLOCKS (CONT.)

```
op maxTimeAdvance : Configuration -> TimeInf [frozen (1)] .
```

```
ceq maxTimeAdvance(CLOCKS CLOCK')  
  = min(maxTimeAdvance(CLOCKS), maxTimeAdvance(CLOCKS'))  
    if CLOCKS /= none and CLOCKS' /= none .
```

```
eq maxTimeAdvance(< C : Clock | running : true, time : R,  
                  rate : RATE >)  
  = (12 - R) / RATE .
```

```
eq maxTimeAdvance(< C : Clock | running : false >) = INF .
```

## MULTIPLE IMPRECISE CLOCKS (CONT.)

Suitable initial state is

```
{< ap : Clock | running : true, time : 0, rate : 5/4 >  
 < seiko : Clock | running : true, time : 0, rate : 1 >  
 < casio : Clock | running : true, time : 0, rate : 99/100 >}
```



## ANOTHER EXAMPLE: POPULATIONS

Many people (cont):

- Time passes uniformly for all living persons
  - everybody birthday same time

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- Time passes uniformly for all living persons
  - everybody birthday same time
- Engagements, weddings, etc. **instantaneous** actions
- Must ensure nobody older than 1000!

## POPULATIONS (CONT.)

Engagement normal **instantaneous** rule:

```
cr1 [engagement] :  
  < P : Person | age : N, status : single >  
  < P' : Person | age : M, status : single >  
=>  
  < P : Person | status : engaged(P') >  
  < P' : Person | status : engaged(P) >  
if N > 15 and M > 15 .
```

## POPULATIONS: TICK RULE

Time can pass by many milliseconds/days/years up to age limit:

```
var PERSONS : Configuration . var R : Time .
```

```
cr1 [tick] :
```

```
  {PERSONS} => {advanceAge(PERSONS, R)} in time R
```

```
  if R <= maxTimeAdvance(PERSONS) [nonexec] .
```

## POPULATIONS: TICK RULE

Time can pass by many milliseconds/days/years up to age limit:

```
var PERSONS : Configuration . var R : Time .  
  
crl [tick] :  
  {PERSONS} => {advanceAge(PERSONS, R)} in time R  
  if R <= maxTimeAdvance(PERSONS) [nonexec] .
```

- advanceAge increases age of each living person by R
- maxTimeAdvance ensures noone gets older than 1000

### Exercise

Define the functions advanceAge and maxTimeAdvance

# OO SPECIFICATIONS

Generalizing: OO system has many instantaneous rules and usually **one** tick rule

```
var STATE : Configuration . var R : Time .
```

```
cr1 [tick] :  
  {STATE} => {timeEffect(STATE, R)} in time R  
  if R <= maxTimeAdvance(STATE) .
```

- `timeEffect(STATE, R)` defines how the elapse of time `R` affects the state `STATE`
- `maxTimeAdvance(STATE)` defines how much time can advance before something must happen

## OO SPECIFICATIONS II

`timeEffect` and `maxTimeAdvance` distribute over objects and messages in a configuration:

```
vars C1 C2 : Configuration .
```

```
ceq timeEffect(C1 C2, R)  
  = timeEffect(C1, R) timeEffect(C2, R)  
  if C1 != none and C2 != none .
```

```
eq timeEffect(none, R) = none .
```

```
ceq maxTimeAdvance(C1 C2)  
  = min(maxTimeAdvance(C1), maxTimeAdvance(C2))  
  if C1 != none and C2 != none .
```

```
eq maxTimeAdvance(none) = INF .
```

These functions must be defined for single objects and messages



Message delays (communication time):

1. Message delay any value  $\in [0, \infty]$
2. Message delay exactly  $\Delta$
3. Message delay **at least**  $\Delta$
4. Message delay between 0 and  $\Delta$
5. Message delay  $\Delta_1$  and  $\Delta_2$

# MODELING MESSAGE DELAYS: CASE 1

Case 1: delay could be **anything**:

- sender sends standard message
- receiver reads standard message
- eq  $\text{timeEffect}(\text{msg}, R) = \text{msg}$  .
- eq  $\text{maxTimeAdvance}(\text{msg}) = \text{INF}$  .

## MODELING MESSAGE DELAYS: CASES 2 AND 3

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```

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- `eq timeEffect(dly(M, R), R') = dly(M, R minus R')`

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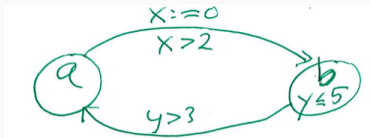
How do we model Case 3 (delay **at least**  $\Delta$ )?

Only change: `eq maxTimeAdvance(dly(M, R)) = INF`

### Exercise

How do we model Cases 4 and 5?

# REPRESENTING TIMED AUTOMATA



State:  $\{location, xVal, yVal\}$

```
vars X Y R : Time .
```

```
rl [tick-a] : {a, X, Y} => {a, X+R, Y+R} in time R [nonexec] .
```

```
crl [tick-b] : {b, X, Y} => {b, X+R, Y+R} in time R  
if R <= 5 - Y [nonexec] .
```

```
crl [ab] : {a, X, Y} => {b, 0, Y} if X > 2 .
```

```
crl [ba] : {b, X, Y} => {a, X, Y} if Y > 3 .
```

# **ANALYSIS IN REAL-TIME MAUDE**

---

- Timed **rewriting**
  - simulate system to time  $T$
- Timed **reachability analysis**
- **LTL** model checking
  - unbounded
  - time-bounded
- **Timed CTL** model checking

- Uses Maude rewriting, search and LTL model checking
- Internal representation of states:
  1.  $\{t\}$  in time *totalDuration*
    - time-bounded analysis
    - reachable state space *infinite*

# INTERNAL REPRESENTATION

- Uses Maude rewriting, search and LTL model checking
- Internal representation of states:
  1.  $\{t\}$  in time *totalDuration*
    - time-bounded analysis
    - reachable state space *infinite*
  2.  $\{t\}$ 
    - “system time” / “duration” abstracted away
    - does not add states
    - analysis *without* time bounds



## RETROGRADE WATCH (AGAIN)

```
(tmod DENSE-CLOCK is pr POSRAT-TIME-DOMAIN .
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    if R' <= 12 - R [nonexec] .

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- “On-the-fly discretization:” time sampling strategies
  - advance time by default value  $\Delta$
  - advance time as much as possible (“event-driven simulation”)

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  - not **executable**
- “On-the-fly discretization:” **time sampling strategies**
  - advance time by default value  $\Delta$
  - advance time **as much as possible** (“**event-driven simulation**”)
- Analysis **incomplete**: all behaviors **not** covered

# SIMULATION

Define time sampling:

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Maude> (set tick def 1 .)
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- analysis w.r.t. this strategy

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Rewriting simulates **one possible** behavior:

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Maude> (trew {clock(0)} in time <= 100 .)
```

# SIMULATION

Define time sampling:

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```

- analysis w.r.t. this strategy

Rewriting simulates **one possible** behavior:

```
Maude> (trew {clock(0)} in time <= 100 .)
```

Result ClockedSystem :

```
{stopped-clock(12)} in time 100
```



## TIME-BOUNDED SEARCH

- Can `{clock(8)}` be reached in time  $\in [23, 25]$ ?

```
Maude> (tsearch {clock(0)} =>* {clock(8)}  
      in time-interval between >= 23 and <= 25 .)
```

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      in time >= 31 .)
```

Solution 1

```
TIME_ELAPSED:Time --> 32
```

- Can `{clock(13)}` be reached?

```
(utsearch [1] {clock(0)} =>* {clock(13)} .)
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- Can `{clock(13)}` be reached?

```
(utsearch [1] {clock(0)} =>* {clock(13)} .)
```

- State `{clock(13)}` not found:

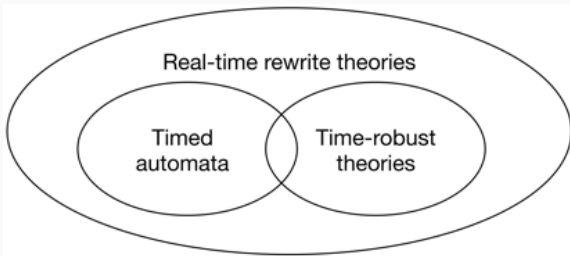
```
(utsearch [1] {clock(0)} =>* {clock(1/2)} .)
```

# SOUND AND COMPLETE UNTIMED ANALYSIS

- Time sampling discretization of dense time
- All behaviors not covered
  - analysis not sound/complete
  - states reached and LTL counterexamples are correct

# SOUND AND COMPLETE UNTIMED ANALYSIS

- **Time sampling** discretization of dense time
- All behaviors **not** covered
  - analysis **not** sound/complete
  - states reached and LTL counterexamples **are correct**
- **Maximal time sampling** analysis sound and complete for **time-robust** models [Ölveczky-Meseguer'06]
  - events at given times
  - atomic propositions not modified by ticks
- Sound/complete analysis for systems beyond timed automata





- So far: **untimed** properties/temporal logic
  - “the airbag must **eventually** deploy after crash detected”
  - “BO **eventually** closes G”

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  - “the airbag must **eventually** deploy after crash detected”
  - “BO **eventually** closes G”
- **Timed** temporal logics
  - “the airbag must deploy **within 10ms** after crash”
  - “BO closes G **within one year** of inauguration”

- Explicit-state **timed CTL** model checker for Real-Time Maude
- **TCTL**: temporal operators with time intervals:  $\exists \phi \mathcal{U}_{[r_1, r_2]} \phi'$ 
  - $\forall \square (\text{crash} \implies \forall \diamond_{\leq 10ms} \text{airbagDeployed})$
  - $\forall \square ((\text{inauguration}(BO) \wedge \text{open}(G)) \implies \forall \diamond_{\leq \text{one year}} \text{closed}(G))$

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- `(mc-tctl {clock(6)} |= EF [ <= than 8 ] clock-is(12) .)`

D. Lepri, E. Ábrahám, P.C. Ölveczky: Sound and complete timed CTL model checking of timed Kripke structures and real-time rewrite theories. Science of Computer Programming 99 (2015)

# INTENDED SEMANTICS

What is the **intended semantics** of a Real-Time Maude model?

$\{clock(R)\} \rightarrow \{clock(R + R')\}$  **in time**  $R'$  **if**  $R' \leq 12 - R$

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- Should  $\forall \diamond_{[1,2]} \text{True}$  hold from  $\{clock(0)\}$ ?
- **Pointwise semantics**
  - only visited states into account
  - $\forall \diamond_{[1,2]} \text{True}$  does **not** hold from  $\{clock(0)\}$

What is the **intended semantics** of a Real-Time Maude model?

$\{clock(R)\} \rightarrow \{clock(R + R')\}$  **in time**  $R'$  **if**  $R' \leq 12 - R$

- Should  $\forall \diamond_{[1,2]} \text{True}$  hold from  $\{clock(0)\}$ ?
- **Pointwise semantics**
  - only visited states into account
  - $\forall \diamond_{[1,2]} \text{True}$  does **not** hold from  $\{clock(0)\}$
- **Continuous semantics**
  - tick rule interpreted as representing continuous process
  - $\forall \diamond_{[1,2]} \text{True}$  **holds** from  $\{clock(0)\}$



# SOUNDNESS AND COMPLETENESS

Soundness and completeness for **maximal time sampling** analyses of **untimed TL** do **not** carry over to **timed CTL**

- maximal time sampling analysis does **not** satisfy  $\exists \diamond_{[1,2]} \text{True}$
- ... or  $\forall \diamond_{[1,2]} \text{True}$

- Continuous and pointwise interpretation

# SOUND AND COMPLETE TCTL MODEL CHECKING

- **Continuous** and **pointwise** interpretation
- **Time-sampling**-based **sound and complete** TCTL model checking for time-robust Real-Time Maude models
  - advance time by

$$\frac{\text{gcd}(\text{numbers in formulas, max-tick durations})}{2}$$

## TIMED CTL MODEL CHECKING (II)

- **Not** reducible to Maude model checking
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- **Not** reducible to Maude model checking
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- **Crossing-the-Bridge** benchmark comparison:

| Initial state | TSMV   | Real-Time Maude |              | RED 7.0 |
|---------------|--------|-----------------|--------------|---------|
|               |        | (pointwise)     | (continuous) |         |
| init(1)       | 0.074  | 0.149           | 1.266        | 0.429   |
| init(10)      | 0.148  | 0.168           | 0.999        | 0.408   |
| init(100)     | 1.443  | 0.168           | 1.012        | 0.404   |
| init(1000)    | 57.426 | 0.327           | 1.014        | 0.426   |
| init+(2)      | 0.191  | 0.746           | 6.864        | 1.044   |
| init+(4)      | 0.280  | 1.772           | 17.752       | 2.153   |
| init+(8)      | 0.759  | 5.227           | 57.580       | 16.912  |
| init+(12)     | 1.080  | 11.198          | 129.957      | 79.319  |
| init+(16)     | 1.515  | 19.620          | 233.414      | 241.098 |

Execution times for the bridge crossing problem (in seconds).

# IN CONTEXT (I)

- Timed automata
  - restricted formalism ...
  - ... many properties decidable
  - state-of-the-art tools: UPPAAL, RED
- Time(d) Petri nets
  - limited tool support
- Timed process algebras

## IN CONTEXT (I)

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  - restricted formalism ...
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  - state-of-the-art tools: UPPAAL, RED
- Time(d) Petri nets
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- Timed process algebras
- IF, TE-LOTOS, etc:
  - separate formalisms for data types, dynamic behavior, and time
  - unclear or non-existing semantics
  - based on **fixed** communication primitives
- MOBY/RT
  - designs specified as PLC-automata
  - translated into **timed automata** for model checking
- BIP (Behavior, Interaction, Priority)
  - “Behavior is described as a Petri net extended with data and functions described in C”

Real-Time Maude:

- simple and intuitive
- expressive
- any data type
- unbounded data structures
- dynamic object/message creation/deletion
- hierarchical structures
- easy to define communication forms



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- expressive
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- hierarchical structures
- easy to define communication forms
  - properties in general **undecidable**
  - discrete abstraction may not exist in general

# APPLICATIONS

---

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Complex data types; unbounded data structures; flexible communication models; hierarchical objects; dynamic object creation/deletion; . . .

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Complex data types; unbounded data structures; flexible communication models; hierarchical objects; dynamic object creation/deletion; ...

Are there systems where Real-Time Maude's expressiveness needed

and

Real-Time Maude analysis yields interesting results?

# CLASSES OF APPLICATIONS

- “Concrete” systems/protocols
- Semantic framework for real-time systems
- Formal analysis tool for other languages
- ...

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- Multicast for **active networks**
  - **50 pages** of use cases
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## Key Real-Time Maude features:

- detailed parametric model of communication
- laaaaarge functions
- multiple class inheritance to combine subprotocols

**CASH**: State-of-the-art scheduling algorithm

- A job can use **more** or **less** time than allocated
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**Key Real-Time Maude feature**: unbounded data structures

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**Key Real-Time Maude features:**

- easy to define “new” model of communication
- complex data types and functions (areas, angles, distances)
- simulation

Megastore: Google's distributed data store



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Key Real-Time Maude features:

- simple and intuitive language
- automatic “testing” highly appreciated
- analysis of **performance** and **correctness**

Modeling and analysis framework for **human multitasking**

- human short-term memory
- attention
- tasks
- ...



Modeling and analysis framework for **human multitasking**

- human short-term memory
  - attention
  - tasks
  - ...
- Will GPS distract driver for more than  $n$  seconds?
  - Will other tasks make driver/pilot forget important things?

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- Found several bugs in embedded car software used by major car makers (Japan)
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- ERMTS/ETCS **railway signaling** and control system
- Leader election for **mobile ad hoc networks**
- EIGRP Cisco routing protocol (Riesco, Verdejo)
- Parts of **NORM** multicast protocol developed by **IETF**

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    - DOCOMO's  $\mathcal{L}$  language
  - timed model transformations
    - Real-Time MOMENT-2
    - e-Motions
  - Orc, Timed Rebeca, . . .

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  - **fixed-point** semantics of **synchronous** languages

## Ptolemy II

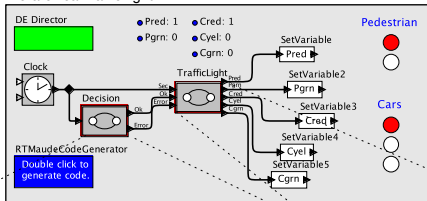
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## Key Maude features:

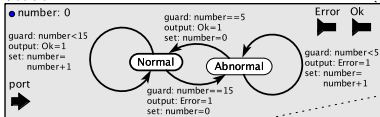
- **hierarchical** configurations
- expressiveness
- unbounded data structures
- **parametric** atomic propositions

# PTOLEMY II: FAULT-TOLERANT TRAFFIC LIGHTS

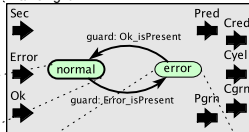
HierarchicalTrafficLight



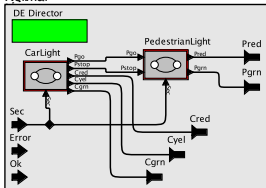
Decision



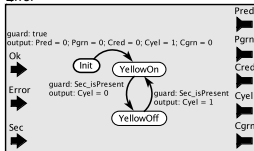
TrafficLight



Normal



Error



Predefined parametric propositions:

*actorId | var<sub>1</sub> = value<sub>1</sub>, ..., var<sub>n</sub> = value<sub>n</sub>*

*actorId @ location*

*actorId | port p is value*

*actorId | port p is status*

Car light will show **only yellow** within time 1 of a failure:

```
AG (( 'HierarchicalTrafficLight . 'Decision |
      port 'Error is present)
    => AF[<= 1] ( 'HierarchicalTrafficLight |
                  'Cyel = 1, 'Cgrn = 0, 'Cred = 0))
```

# ANALYZING PTOLEMY II MODELS WITHIN PTOLEMY

codeDirectory:

generatorPackage:

generateComment:

inline:

overwriteFiles:

run:

Simulation bound:

Safety Property:

Alternation Property:

Error Handling:

---

Code Generator Commands

```
Check
mc-tctl {init} |= AG (('HierarchicalTrafficLight . 'Decision)|(port 'Error is
  present)implies AF[<= than 1] 'HierarchicalTrafficLight |('Cyel = # 1,'Cgrn
  = # 0,'Cred = # 0)) .
in PTOLEMY-MODELCHECK with mode maximal time increase

Checking equivalent property:
mc-tctl {init} |= not (E tt U[>= than 0] ('HierarchicalTrafficLight .
  'Decision)|(port 'Error is present) and (E not 'HierarchicalTrafficLight |
  'Cgrn = # 0,'Cred = # 0,'Cyel = # 1)U[> than 1] tt) .

Property not satisfied
```

All Done

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  - value added to domain-specific analysis
- Useful both as simulation tool and model checker
- Semantics and analysis tool for modeling languages
  - model checker for free for those languages

# **IMMEDIATE RESEARCH CHALLENGES**

---

# COMBINING REAL-TIME AND PROBABILITIES

- Large distributed systems often **real-time** and **probabilistic**

- Large distributed systems often **real-time and probabilistic**
- PVeStA and MultiVeStA: **statistical model checking**
  - estimate value of expression with statistical guarantees
  - **scalable** formal method
  - apply to **fully probabilistic** rewrite theories

Exists:

1. Formal model for probabilistic real-time rewrite theories

[Bentea-Ölveczky'11]

# COMBINING REAL-TIME AND PROBABILITIES (CONT.)

Exists:

1. Formal model for probabilistic real-time rewrite theories

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2. Obtain **fully probabilistic** “real-time” OO models [Meseguer et al'12]:
  - message delay sampled probabilistically from **dense** interval
    - zero probability that two message-triggered actions enabled same time
  - estimate performance, etc, of **cloud computing systems** and **DoS defense mechanisms**



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  - message delay sampled probabilistically from **dense** interval
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Need: theoretical model and language/tool support

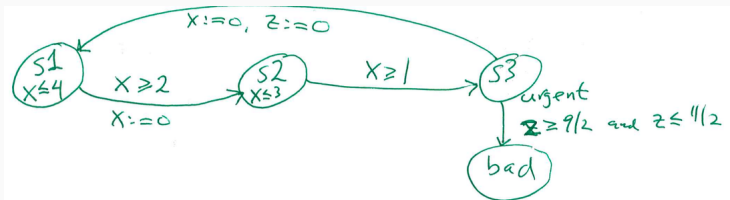
- larger class of systems (message-triggered; flat OO; ad-hoc timing)
- automatic transformation to PVeStA

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- “Real-Time Maude modulo SMT”
  - full reachability analysis for timed automata (?)

# REWRITING MODULO SMT: COMPLETE REACHABILITY FOR TIMED AUTOMATA (?)



```
vars x y z : Real .
```

```
crl < s1 ; x ; z > => < s2 ; 0/1 ; z > if x >= 2/1 = true .
```

```
crl < s1 ; x ; z > => < s1 ; x + y ; z + y > if x + y <= 4/1 =
```

```
crl < s2 ; x ; z > => < s3 ; x ; z > if x >= 1/1 = true .
```

```
crl < s2 ; x ; z > => < s2 ; x + y ; z + y > if x + y <= 3/1 = t
```

```
crl < s3 ; x ; z > => < bad ; x ; z > if z >= 9/2 and z <= 11/2
```

```
rl < s3 ; x ; z > => < s1 ; 0/1 ; 0/1 > .
```

# REWRITING MODULO SMT: COMPLETE REACHABILITY FOR TIMED AUTOMATA (?) (CONT.)

Region reachable from **some** initial **x**-value?

```
Maude> smt-search [1] < s1 ; x ; 0/1 > =>* < bad ; y ; z >
      such that z > y and z > 2/1 = true .
```

Solution 1

rewrites: 26 in 21ms cpu (21ms real) (1233 rewrites/second)

state: < bad ; 0/1 + #2-y:Real ; 0/1 + #1-y:Real + #2-y:Real >

empty substitution

where z > y and z > 2/1 and x + #1-y:Real <= 4/1 and x + #1-y:Real >= 2/1 and 0/1 + #2-y:Real >= 1/1 and (0/1 + #1-y:Real + #2-y:Real >= 9/2 and 0/1 + #1-y:Real + #2-y:Real and z == 0/1 + #1-y:Real + #2-y:Real)

- Peter C. Ölveczky: [Real-Time Maude and its Applications](#). In Proc. WRLA 2014, volume 8663 of Lecture Notes in Computer Science, Springer, 2014.
- Peter C. Ölveczky and José Meseguer: [Semantics and Pragmatics of Real-Time Maude](#). In volume 20(1/2) of Higher-Order and Symbolic Computation, Springer 2007.

## EXERCISE

In rate-monotonic scheduling, you have given a set of periodic tasks, each with an **execution time** and **period**. When its period ends, it starts a new period. Within each period, it must execute for a total of its **execution time**. We assume that we have only one processor. The task with the shortest period has the highest priority to execute, and can preempt an executing task with a lower priority. Assume that you can have tasks with the same period/priority. Specify the rate-monotonic scheduling algorithm in Real-Time Maude, and try model checking of a few examples to check whether your task set is schedulable.